# The Cole-Moore Effect in Nodal Membrane of the Frog Rana Ridibunda: Evidence for Fast and Slow Potassium Channels

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Summary. The K conductance  $(g_K)$  kinetics were studied in voltage-clamped frog nodes (Rana ridibunda) in double-pulse experiments. The Cole-Moore translation for  $g_K - t$  curves associated with different initial potentials (E) was only observed with a small percentage of fibers. The absence of the translation was found to be caused by the involvement of an additional, slow,  $g_K$  component. This component cannot be attributed to a multiple-state performance of the K channel. It can only be accounted for by a separate, slow K channel, the fast channel being the same as the  $n^4$  K channel in R. pipiens.

The slow K channel is characterized by weaker sensitivity to TEA, smaller density, weaker potential (E) dependence, and somewhat more negative E range of activation than the fast K channel. According to characteristics of the slow K system, three types of fibers were found. In Type I fibers (most numerous) the slow K channel behaves as an  $n^4$  HH channel. In Type II fibers (the second largest group found) the slow K channel obeys the HH kinetics within a certain E range only; beyond this range the exponential decline of the slow  $g_K$  component is preceded by an E-dependent delay, its kinetics after the delay being the same as those in Type I fibers. In Type III fibers (rare) the slow K channel is lacking, and it is only in these fibers that the Cole-Moore translation of the measured  $g_K - t$  curves can be observed directly.

The physiological role of the fast and slow K channel in amphibian nerves is briefly discussed.

**Key words:** Ranvier node, potassium currents, Hodg-kin-Huxley kinetics, potassium channel conductance states.

Quantitative descriptions of the K conductance  $(g_K)$  kinetics in the node of Ranvier in terms of the Hodgkin-Huxley (HH) model (Hodgkin & Huxley, 1952) were given by Dodge (1963) and Frankenhaeuser (1963) for two different amphibian species. Dodge found no marked departure from the HH formalism in the frog *Rana pipiens*, while Frankenhaeuser was compelled to conclude that for the toad *Xenopus laevis* this formalism "is incomplete and, strictly considered, it is not correct."

Recently, in two other cases studied in detail, R. ridibunda and R. esculenta, it has been established that the  $g_K$  kinetics behave like those in X. laevis (see references below). No explanation for this strange difference between R. pipiens and other amphibian species has so far been offered. Meanwhile the answer to the question as to why the  $g_K$  kinetics in some (and probably most) amphibian nodes differ from the HH formalism may lead to a better understanding of the K channel performance.

Within the HH framework the K channel conductance is controlled by a number (x) of identical gating subunits, each of which can be only in one of two states, either closed  $(n_c)$  or open  $(n_o)$ , the open-closed transition obeying the first-order kinetics:

$$n_c \frac{a_n}{\sqrt{b_n}} n_o \tag{1}$$

$$\frac{dn}{dt} = a_n(1-n) - b_n \cdot n \tag{2}$$

where  $a_n$  and  $b_n$  are rate constants dependent on the membrane potential (E) but not on time (t). Following a step change in E from an initial value,  $E_1$ , to a final value,  $E_2$ , the relaxation of a gating subunit from an equilibrium state at  $E_1$ ,  $n_\infty(E_1)$ , to a new equilibrium state at  $E_2$ ,  $n_\infty(E_2)$ , will proceed as

$$n(t) = n_{\infty}(E_2) - [n_{\infty}(E_2) - n_{\infty}(E_1)] \exp(-t/\tau_n)$$
 (3)

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where  $n_{\infty} = a_n (a_n + b_n)^{-1}$  and  $\tau_n = (a_n + b_n)^{-1}$ . As with the rate constants  $a_n$  and  $b_n$ , the relaxation time  $\tau_n$  is determined by  $E_2$  only: at a given test potential  $E_2$  it should be the same, whatever the prepulse  $E_1$  was. The gate (and the K channel) is open only when all x subunits are in the state  $n_o$ . The overall  $g_K$  of a K channel population can then be described as

$$g_{\mathbf{K}}(t) = \bar{g}_{\mathbf{K}} \, n^{x}(t) \tag{4}$$

where  $\bar{g}_{K}$  is the maximum  $g_{K}$ .

The HH formalism for  $g_K$  kinetics is thus based on the single first-order variable n, and this fact allows a ready testing of the validity of this formalism. Indeed, Eq. (3) for n can be rewritten as

$$n(t) = n_{\infty}(E_2) \left[ 1 - \exp\left(-(t - \Delta t)/\tau_n\right) \right]$$
 (5)

for depolarizing E steps, when  $E_1 < E_2$  and  $n_{\infty}(E_2) < n_{\infty}(E_1)$ , with

$$\Delta t = \tau_n \cdot \ln \frac{n_{\infty}(E_2)}{n_{\infty}(E_2) - n_{\infty}(E_1)} \tag{6}$$

and

$$n(t) = n_{\infty}(E_2) \left[ 1 + \exp\left(-(t + \Delta t)/\tau_n\right) \right] \tag{7}$$

for repolarizing E steps, when  $E_1 > E_2$  and  $n_{\infty}(E_1) > n_{\infty}(E_2)$ , with

$$\Delta t = \tau_n \cdot \ln \frac{n_{\infty}(E_2)}{n_{\infty}(E_1) - n_{\infty}(E_2)}.$$
 (8)

Thus changing of initial conditions (prepulse  $E_1$ ) should lead to parallel shift of the n-t curve and, consequently, of the  $g_K-t$  curve along the t-axis if the test pulse  $E_2$  remains constant. Therefore in the HH formalism the  $g_K$  kinetics should not depend on initial conditions, i.e., on the parameters of  $E_1$ . Hill and Chen (1972) and Chen (1976) extended the single-conductance HH model to multiple-conductance models, k-models. Since k-models are formally the same as in HH, the Cole-Moore translation should take place in these models as well.

Cole and Moore (1960) experimentally confirmed the translation in squid axon membrane. Dodge (1963) came to the same conclusion with R. pipiens, and this seems to be, so far, the only known example of the kind for amphibian myelinated fibers. In X. laevis both  $b_n$  (Frankenhaeuser, 1963) and  $a_n$  (see Makovsky (1975) for analysis of Frankenhaeuser's (1962) data) depend on prepulse duration. The dependence of  $g_K$  on initial conditions has also been reported for R. ridibunda in our preliminary publications (Ilyin et al., 1973, 1974a, b, 1977) and R. esculenta (Palti, Ganot & Stämpfli, 1976; Ganot, Palti & Stämpfli, 1978).

In this paper we show that in R. ridibunda node the dependence of  $g_K$  kinetics on the prepulse amplitude at repolarizations is the result of activation of two uncoupled  $g_K$  components, a fast and a slow, and we present evidence that at depolarizations the components obey  $n^4$  kinetics but with different time and voltage dependencies of the HH variables. We attribute the slow  $g_K$  component to a slow K channel of the HH type, the fast K channel being most probably the same as in K. K

#### Materials and Methods

#### Preparation

Single large (15-20 µm) fibers were dissected from the sciatic nerve of the frog *R. ridibunda*. No effort was made to distinguish, between motor and sensory fibers.

## Experimental technique

The voltage-clamp method used has been described elsewhere (Lonskii, Ilyin & Malov, 1972). It had a great deal in common with that of Nonner (1969), the main distinctions being:

- 1. Large internodal resistances were achieved with air gaps of fixed widths.
- 2. The liquid pool on the recording side was carefully shielded, and the shield was connected to the output of a cathode follower with a coefficient of amplification 0.998. This made it possible to reduce the input capacity to about 0.015 pF and to clamp the membrane potential in less than 15  $\mu$ sec to within 1-2%. Further details can be found in Lonskii et al., 1972.

#### Solutions

Composition of the solution used (adjusted to pH 7.4) is given in Table 1. The temperature of the solutions bathing the node was 15-18 °C.

Solution 1 was used to check the functional condition of the node. Solution 2 was used for liquid pools for fiber cut ends on both sides of the node.

K ion accumulation in the perinodal space during outwardly directed  $I_{\rm K}$  (Dubois & Bergman, 1975) may lead to an appreciable difference between time courses of  $g_{\rm K}$  and  $I_{\rm K}$  (Adam, 1973; Adelman, Palti & Senft, 1973). Therefore, all the experiments intended to measure  $g_{\rm K}-t$  curves for subsequent quantitative analysis were performed in high K solution 4. The further advantages of high K solution were large and faithful  $I_{\rm K}$  currents associated with repolarizing steps ( $I_{\rm K}$  tails). This fact was of paramount importance in the present study because the model proposed is mostly based on evidence obtained from quantitative analysis of  $I_{\rm K}-t$  curves measured in various double-pulse repolarization experiments.

# Experimental Procedure

Programs of pulses applied to a node are described in the text and figure legends. Successive runs of a program were spaced at 2 sec. In between the runs the node was held at resting potential  $(E_{\rm R})$  assumed to be  $-70\,{\rm mV}$ . Prepulse  $E_1$  was preceded by a holding potential  $E_0$  with an amplitude of about  $-100\,{\rm mV}$  and a duration

Table 1. Composition of solution around the node (mm)

Solution	KCl	NaCl	CaCl <sub>2</sub>	Tris Cl	TTX	TEA
1	2.5	125.5	2.5	5.0	0	0
2	128	0	0	5.0	0	0
3	2.5	125.5	2.5	5.0	$3 \cdot 10^{-4}$	0
4	128	0	2.5	5.0	$3 \cdot 10^{-4}$	
5	2.5	125.5	2.5	5.0	$3 \cdot 10^{-4}$	20
6	128	0	2.5	5.0	$3 \cdot 10^{-4}$	20

TTX: tetrodotoxin; TEA: tetraethylammonium bromide. In solution 2 KF was sometimes used instead of KCl.

of 100 msec (see, e.g., inset in Fig. 4). To determine the absolute membrane potential (E) of a node, the node was destroyed at the end of experiment by a strong positive pulses and the residual potential was subtracted from all the pulses of the programs used in this experiment. E is reported as inside minus outside potential.

## Obtaining the net Ik

Each program of pulses was repeated twice: first in a working solution (3 or 4) and then in its counterpart solution (5 or 6, respectively) containing 20 mm TEA (see Table 1). "The potassium currents  $I_{\rm K}$ " are the net currents obtained after subtraction of the currents in solutions 5 or 6 from the corresponding currents in solutions 3 or 4. By this procedure we excluded not only the currents of capacitative surge and ohmic leak but also the exponentially decaying current (Hille, 1967b), unaffected by TTX and TEA, observed in some fibers.

#### Analysis of IK

The steady-state value of  $I_{\rm K}(I_{\rm K_{\infty}})$  at repolarizations was measured at the end of a 100-msec test pulse. An exponential time sweep was used to show both the fast and slow portions of  $I_{\rm K}$  on the same record. The photographic records of currents were digitized by an A/D converter PUOS (Russian index). The net  $I_{\rm K}-t$  curves were recalculated into linear time scale and analyzed either graphically or on a computer by fitting to the observations the modified HH Eq. (17) with the method of least squares. Minimization of variance was performed with the method of steepest descent. Special attention was given to test that a local minimum had not been mistaken for the absolute minimum being sought (Brent, 1973).

## Results and Analysis

We shall first consider the results obtained in the repolarization experiments because they are important for an understanding of the depolarization data.

## 1. K Currents at Repolarization: Results

In all repolarization experiments the node under investigation was in high K solution 4. About 400 nodes were examined, and three basic types of  $I_{\rm K}$  currents (tails) were identified. Each type is described

under separate paragraphs. At present we cannot give the exact evaluation of the occurrence of each type because not all the material obtained was treated quantitatively and many  $I_{\rm K}$  tails were classified by sight.

1.1. Type I Fibers. Such fibers were the most frequent. A typical case is presented at the top of Fig. 1: five  $I_K$  tails associated with five different prepulses  $E_1$  and a constant test pulse  $E_2$  are shown. It is seen that each

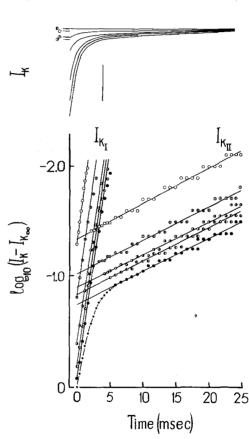


Fig. 1. The Cole-Moore test for repolarization in a Type I fiber. Above:  $I_K$  tails associated with E steps to  $E_2 = -106$  mV from different  $E_1$  (downwards from the base-line): -60, -48, -30, -1, +55 mV.  $I_K$  levels, immediately before a step, at these  $E_1$  values are indicated by symbols O, O, O, O, O, respectively. Duration of  $E_1$ , 40 msec. (For other details, see text and inset in Fig. 4.) Note that the tails are nonparallel. 128 mm K Ringer plus  $3 \cdot 10^{-4}$  mm TTX. Leakage current subtracted. Calibration current bar,  $5 \cdot 10^{-9}$  A. Time axis as below. Below: graphical analysis of the  $I_{\rm K}$ tails above.  $I_{K_{\infty}}$ :  $I_{K}$  value at t = 100 msec. Only the largest  $(I_{K} - I_{K_{\infty}})$ tail, associated with  $E_1 = +55$  mV, is fully represented, by way of illustration, by the undermost dashed-dotted curve continued as solid curve. The maximum value of this tail (at t=0) is normalized to 1. The other four  $(I_K - I_{K_\infty})$  tails are only represented by their components  $I_{\mathbf{K}_1}$  and  $I_{\mathbf{K}_{11}}$ . Symbols relate to  $E_1$  values before a step, as above. Note that  $I_{\mathbf{K}_1}-t$  and  $I_{\mathbf{K}_{11}}-t$  curves are parallel (within their families). For values of relaxation times  $\tau_{\mathbf{K}_1}$  and  $\tau_{\mathbf{K}_{11}}$ , see Table 2 (columns 3 and 6, respectively). Node 371

tail consists of a fast and a slow portion. In accordance with Eqs. (7)–(8), the  $I_{\rm K}-t$  curves shift to the left along the t-axis with more negative  $E_1$ , but the shifts are nonparallel.

However, from graphical analysis at the bottom of Fig. 1 it is clear that each  $I_{\kappa}$  tail can be divided into a fast  $(I_{K_1})$  and a slow  $(I_{K_{11}})$  component, which do shift in parallel along the t-axis and are the exponential functions of time. This means that their associated relaxation times  $\tau_{K_I}$  and  $\tau_{K_{II}}$  are independent of the prepulse amplitude, i.e., the behavior of each component is controlled by a first-order variable. In this experiment there were nine different values of  $E_1$ . The relaxation times obtained are collected in Table 2 (column 3 for  $\tau_{K_1}$  and column 6 for  $\tau_{K_2}$ ). For this node, at  $E_2 = -106 \,\text{mV}$ ,  $\tau_{K_1}$  was  $0.95 \pm 0.03 \,\text{msec}$  and  $\tau_{\rm Kn}$  was  $14.2 \pm 0.7$  msec (mean  $\pm$  sD for n=9). It should be noted that  $\tau_{K_{II}}$  (as  $\tau_{K_{I}}$ ) is the same regardless the direction of  $I_K$  during prepulse. This means that  $I_{K_{\Pi}}$  cannot be due to washing out of excess K ions

**Table 2.** Time constants  $\tau_{K_1}$ ,  $\tau_{K_{11}}$  and  $\tau_{K}$  (for a node in Fig. 10) obtained from graphical analysis of tails of potassium currents associated with repolarizing steps from different conditioning potentials  $E_1$  to the same test potential  $E_2$ 

1	2	3	4	5	6	7	8
E <sub>1</sub> (mV)	$\tau_{\mathbf{K}}$	τ <sub>K1</sub> (msec)	τ <sub>κι</sub> (msec)	$ au_{\mathbf{K}_{\mathtt{I}}}$ (msec)	τ <sub>KII</sub> (msec)	τ <sub>KII</sub> (msec)	τ <sub>KII</sub> (msec)
+65			1.05	1.04		22.2	21.7
+60	0.99						
+55		0.96			14.3		
+46			1.05	1.08		20.0	22.9
+42	0.99						
+36			1.03	1.00		23.8	19.5
+29		0.96			15.0		
+23	1.00						
+16			1.00	0.90		24.0	20.2
+10	1.02	0.95			14.8		
+4			1.03	1.01		20.7	22.7
+1	1.00						
-1		0.96			14.2		
-10			1.04	0.86		19.8	20.1
-14	1.00						
-19		0.94	1.05	1.03	13.1	22.6	21.6
-26	0.96		0.90	1.00		22.7	19.8
-30		0.98			14.9		
-35	1.00		1.00	1.05		20.8	20.3
-40		0.89			13.4		
-42	0.98		1.06	1.04		22.5	20.0
-48	0.99	0.97			14.2		
	1.00						
-60	1.01	0.96	1.05	1.03	13.5	20.5	20.4
Mean		0.95	1.02	1.00	14.2	21.7	20.8
$\pm sD$	$\pm 0.015$	$\pm 0.03$	$\pm 0.05$	$\pm 0.07$	$\pm 0.7$	$\pm 1.5$	$\pm 1.2$

Column 2: node 518;  $E_1$ : 50 msec duration;  $E_2$ : -98 mV. Column 3, 6: node 371;  $E_1$ : 40 msec duration;  $E_2$ : -106 mV. Column 4, 7: node 253;  $E_1$ : 20 msec duration;  $E_2$ : -100 mV. Column 5, 8: node 253;  $E_1$ : 500 msec duration;  $E_2$ : -100 mV.

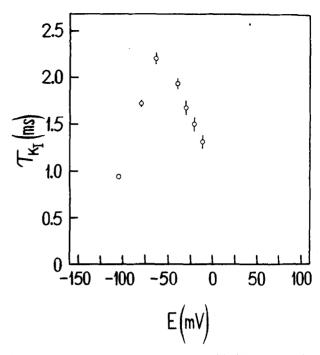


Fig. 2. The relationship  $\tau_{K_1}$ —E measured with different prepulses  $E_1$ . E values on the abscissa are values of the test potential  $E_2$  used; duration of  $E_1$ , 40 msec. Prepulses  $E_1$  were:

Bars indicate sD from the mean. For  $\tau_{K_1}$  (-106 mV) sD is too small to be shown on the scale (0.95  $\pm$ 0.03 msec, see Table 2, column 3). The same experiment as in Fig. 1

accumulated in the perinodal space. Moreover, the high K solution we used to bathe the node ruled out the possibility of K ion accumulation (see Figs. 6 and 7).

A similar set of pulses was applied to this node six more times with six other test pulses  $E_2$ . The mean relaxation times obtained, with their SD, are shown in Fig. 2 ( $\tau_{\rm K_I}$ ) and Fig. 3 ( $\tau_{\rm K_I}$ ). It is seen that the relaxation times do not depend on  $E_1$  at any  $E_2$ . An increase in SD with  $E_2$  in Figs. 2 and 3 must be attributed to progressively less accurate measurements of  $\tau_{\rm K_I}$  and  $\tau_{\rm K_{II}}$  as  $E_2$  values increase due to smaller  $I_{\rm K}$  tails and progressively lesser number of independent measurements (see legend to Fig. 2).

The other way to change initial conditions is to vary the prepulse duration. We only used long prepulses  $E_1$ . Some results are shown in Fig. 4. The

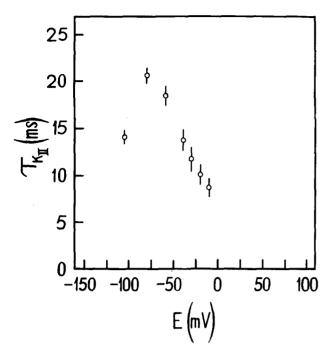


Fig. 3. The relationship  $\tau_{K_{II}} - E$  measured with different prepulses  $E_1$ . All the details are as in Fig. 2. The experiment is the same as in Figs. 1 and 2

program of E steps was here analogous to that in Fig. 1, but prepulses  $E_1$  were 20 and 500 msec long. It seen again that  $I_{\rm K}$  tails can be resolved into two components,  $I_{\rm K_1}$  and  $I_{\rm K_{II}}$ , which shift along the t-axis with changing of  $E_1$  amplitude. The changing of  $E_1$  duration results in a parallel shift of  $I_{\rm K_{II}}$  and practically no shift of  $I_{\rm K_{II}}$ . This means that  $I_{\rm K_{II}}$  is and  $I_{\rm K_{II}}$  is not inactivated by long prepulses  $E_1$  and that neither  $\tau_{\rm K_{II}}$  nor  $\tau_{\rm K_{II}}$  depend on prepulse duration (see Figs. 5-7 and Table 2).

Table 2 presents quantitative data illustrating independence of relaxation times of both components on prepulse duration. With  $E_1$  at 20 msec,  $\tau_{K_I}$  was  $1.02\pm0.05$  msec (column 4), and with  $E_1$  at 500 msec, it was  $1.00\pm0.07$  msec column 5);  $\tau_{K_{II}}$  values were, respectively,  $21.7\pm1.5$  and  $20.8\pm1.2$  msec (columns 7 and 8) (mean  $\pm$  sp for n=11).

In Fig. 5 the instantaneous amplitudes of  $I_{\mathbf{K_I}}$  and  $I_{\mathbf{K_I}}$  from the above experiment are plotted against  $E_1$ . They are presented as  $g_{\mathbf{K_{I\infty}}}$  and  $g_{\mathbf{K_{II\infty}}}$  since, first, there being no K ion accumulation under these conditions (see Figs. 6 and 7), the time courses of  $g_{\mathbf{K}}$  and  $I_{\mathbf{K}}$  are the same and, second, there is every reason to believe that  $I_{\mathbf{K_I}}$  is fully activated during  $E_1$  of 20 msec duration (see Figs. 2 and 8A), and  $I_{\mathbf{K_{II}}}$  is fully activated during  $E_1$  of 500 msec duration (see Figs. 3 and 8B). From Fig. 5 it can be seen that a long prepulse reduces  $g_{\mathbf{K_I}}$  in this node to 0.2 of its initial value (Fig. 5A) but does not affect  $g_{\mathbf{K_{II}}}$  (Fig. 5B). A slight

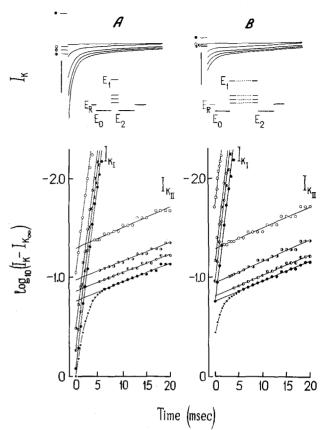


Fig. 4. The Cole-Moore test at repolarizations in a Type I fiber with prepulses of 20 msec (A) and 500 msec (B). Above:  $I_{\rm K}$  tails associated with steps from  $E_1$  (downwards from the base-line): -60, -42, -19, and +65 mV to  $E_2=-100$  mV.  $I_{\rm K}$  levels immediately before a step at these  $E_1$  values are indicated by symbols 0,  $\bullet$ , and  $\bullet$ , respectively. Inset: the program of stimuli. (For other details, see text.) 128 mM K Ringer solution plus  $3 \cdot 10^{-4}$  mM TTX. Leakage current subtracted. Calibration current bar,  $5 \cdot 10^{-9}$  A. The time axis was as below. Below: graphical analysis of the  $I_{\rm K}$  tails above. All the details are as in Fig. 1. Note that the sole effect of a long conditioning prepulse consists of a reduction of the magnitude of a fast current  $I_{\rm K_{1}}$ . For values of time constants, see Table 2, columns 4 and 7 (short  $E_1$ ) and columns 5 and 8 (long  $E_1$ ). For relative values of amplitudes of instantaneous currents  $I_{\rm K_{10}}$  and  $I_{\rm K_{100}}$  on linear scale, see Fig. 5A and B, respectively. Node 253

increase in  $g_{K_{II}\infty}$  at large and negative prepulses in Fig. 5B may certainly be explained by the assumption that it takes longer than 20 msec to fully activate the slow component  $g_{K_{II}}$  by negative potentials.

Figures 6 and 7 show another type of inactivation experiment. Full instantaneous values of  $I_{\rm K}$  were measured here at different test potentials  $E_2$  (Fig. 6) and divided into  $I_{\rm K_I}$  and  $I_{\rm K_{II}}$  (Fig. 7; the procedure is described below).  $E_1$  (67 mV) was at 50 and 500 msec. Again, during 500 msec  $I_{\rm K_{II}}$  did not change while  $I_{\rm K_{I}}$  fell to 0.4 of its initial value. Figure 6 shows that  $E_{\rm K}$  does not change during long polarization by a positive pulse as large as 67 mV. This means that the reduction of  $I_{\rm K_{I}}$  in the above experiments is really

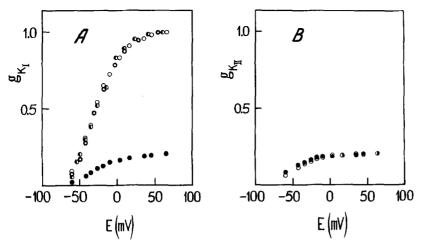
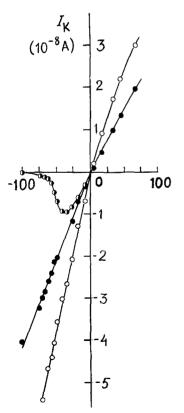
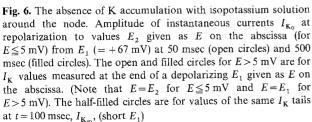
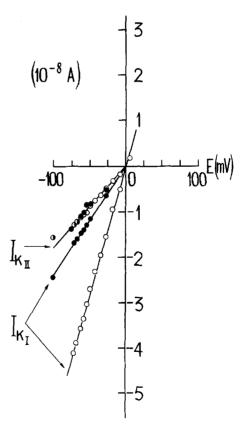


Fig. 5. Instantaneous conductances  $g_{K_1}(A)$  and  $g_{K_{IR}}(B)$  measured at repolarization from values  $E_1$  given by abscissa to  $E_2 = -106$  mV ( $\bullet$ ), -100 mV ( $\bullet$ ), -98 mV ( $\bullet$ ). (A):  $g_{K_I}$  for:  $\bullet$ , node 371,  $E_1$  40 msec (see also Fig. 1);  $\bullet$ , node 518,  $E_1$  50 msec (see also Fig. 10);  $\bullet$ , node 253,  $E_1$  20 msec (see also Fig. 4A);  $\bullet$ , node 253,  $E_1$  500 msec (see also Fig. 4B). The maximum conductances  $g_{K_I}$  of all three nodes are normalized to 1. All other details as in Fig. 1, 4 and 10. Note that the plot in A reflects the potential dependence of the steady-state conductance  $g_{K_I}$ ,  $g_{K_{II}\infty}$ , and in B the plot given by filled circles reflects the potential dependence of the steady-state conductance  $g_{K_{II}}$ ,  $g_{K_{II}\infty}$ 







**Fig. 7.** Amplitudes of instantaneous currents  $I_{\rm Kro}$  and  $I_{\rm Kro}$  at repolarization from  $E_1=+67~\rm mV$  to values  $E_2$  given as E on the abscissa. (For details of construction, see text.) 128 mM KCl Ringer plus  $3\cdot 10^{-4}~\rm mM$  TTX. Node 508-2. The same experiment as in Fig. 6.

due to inactivation; furthermore, the reduction of  $I_{K_I}$  occurs with constant  $E_{K_I}$  (Fig. 7).

The overall kinetics of  $I_K$  tails in Type I fibers can be expressed as

$$I_{K}(t) = I_{K_{II}} \exp(-t/\tau_{K_{I}}) + I_{K_{II}} \exp(-t/\tau_{K_{II}}) + I_{K_{m}}$$
 (9)

where  $I_{\rm K_{10}}$  and  $I_{\rm K_{II0}}$  are  $I_{\rm K_1}$  and  $I_{\rm K_{II}}$  as in Figs. 1 and 4 at t=0, and  $I_{\rm K_{\infty}}$  is, as usual,  $I_{\rm K}$  at t=100 msec. Now within the range of  $E_2$  where  $I_{\rm K_{\infty}}$  values were neglegibly small (see Fig. 6) the corresponding  $I_{\rm K_{II0}}-E_2$  and  $I_{\rm K_{II0}}-E_2$  characteristics were straight lines through  $E_2=E_{\rm K_1}=E_{\rm K_{II}}=0$ . But with those  $E_2$  values where  $I_{\rm K_{\infty}}$  values were perceptibly large (see Fig. 6) (and it will be noted that  $I_{\rm K_{I0}}$  and  $I_{\rm K_{II0}}$  fall with increase in  $E_2$ ) the same linear dependences took place only for plots ( $I_{\rm K_{I0}}+I_{\rm K_{I\infty}}$ )— $E_2$  and ( $I_{\rm K_{II0}}+I_{\rm K_{II\infty}}$ )— $E_2$ ,  $I_{\rm K_{II\infty}}+I_{\rm K_{II\infty}}=I_{\rm K_{\infty}}$  in Eq. (9). The values of  $I_{\rm K_{IO}}$  and  $I_{\rm K_{II0}}-E_1$  and  $I_{\rm K_{II0}}-E_1$  characteristics for this node, with  $E_2=-100$  mV (i.e., with negligibly small  $I_{\rm K_{\infty}}$ ), and  $E_1$  duration 50 and 500 msec, respectively.

The relaxation times  $\tau_{\rm K_I}$  and  $\tau_{\rm K_{II}}$  of the components  $I_{\rm K_I}$  and  $I_{\rm K_{II}}$  from the above experiment are shown in Fig. 8A and B, respectively. One can see that they do not depend on prepulse duration. One can also conclude that inactivation of  $I_{\rm K_I}$  proceeds independently of its activation.

The behavior of an *i*-th component of  $g_K$  such as observed in the above experiments can be fully de-

scribed with the use of two functions:  $g_{K_{Im}}(E)$  and  $\tau_{\kappa}(E)$ . However, in our experiments the concrete shapes of these functions markedly varied from fiber to fiber, especially those relating to the slow component  $g_{K_{II}}$ . Thus the relative value fo  $\bar{g}_{K_{II}}$  with respect to the value of  $\bar{g}_{K_I}$  ranged from 0.2 to 0.8 (being mostly between 0.2 and 0.3). The maximum values of  $\tau_{K_{II}}$  were scattered within the range of 15-30 msec at 15–18 °C. The positions of  $g_{K_{\text{H}m}} - E$  curves on the E-axis and their slopes also varied markedly, but these slopes were always considerably less steep than the slopes of  $g_{K_{10}}-E$  curves. As for the fast component  $g_{K_1}$ , the parameters characterizing its activation varied to a much lesser degree, the main source of variability being the degree of inactivation during the action of prepulse, which varied considerably from fiber to fiber (cf. Figs. 5A and 7). This inactivation corresponds to fast K inactivation described by Schwarz and Vogel (1971) in X. laevis. There is also a slow K inactivation in R. ridibunda nerves similar to that in X. laevis as described by Schwarz and Vogel, but we shall not deal with it here.

1.2. Type II fibers. This was the second largest group. Its distinctive feature is the behavior of the slow component  $I_{K_{\Pi}}$ .

Figure 9 illustrates a typical case. Here  $E_2$  was -104 mV and  $E_1$  varied from 52 to -62 mV. It can be seen that  $I_K$  tails associated with  $E_1 = -62$  and

O

50

100

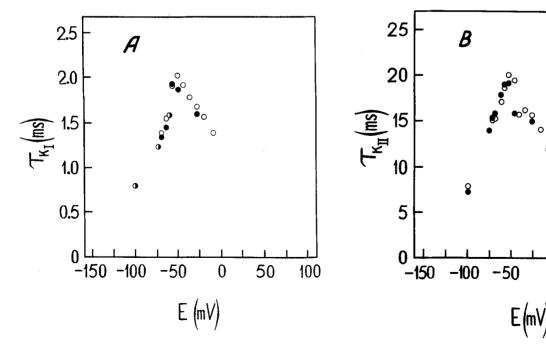


Fig. 8. The relationships  $\tau_{K_1} - E$  (A) and  $\tau_{K_{11}} - E$  (B) measured with prepulses  $E_1$  of two different durations. The amplitude of  $E_1$  was  $+67 \,\mathrm{mV}$ ; the duration of  $E_1$  was  $50 \,\mathrm{msec}$  (open circles) and  $500 \,\mathrm{msec}$  (filled circles). The values of E on the abscissa are values of the test potential  $E_2$  used. The experiment is the same as in Figs. 6 and 7

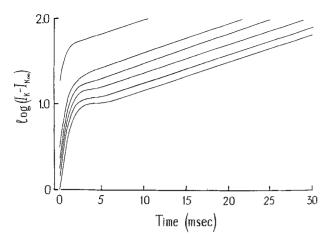


Fig. 9. The Cole-Moore test for repolarization in a Type II fiber.  $E_1$  (in the downward direction) were -62, -42, -32, -3, +8 and +53 mV.  $E_2$  was -104 mV. The instantaneous amplitude of the maximum current (associated with a step from  $E_1 = +53$  mV) is normalized to 1. All the other details are as in Fig. 1. Note that the  $I_{\rm K}$  tails associated with  $E_1$  equal to -62 and -42 mV behave as those in Fig. 1 while the  $I_{\rm K}$  tails associated with  $E_1$  equal to -32, -3, +8 and +53 mV have a shoulder lengthening with  $E_1$ . Node 372

 $-42 \,\mathrm{mV}$  have the fast and slow components of the same type as in the bottom graphs of Figs. 1 and 4. However, as  $E_1$  is shifted towards more positive values there appears a delay in the decay of the slow component, which increases with  $E_1$ . The fast component (when separated) was in all respects identical to that in the bottom graphs of Figs. 1 and 4 (not shown); after subtraction of the fast component, the delay in the decline of the slow component was much more pronounced (not shown).

It should be noted that after the delay the slow components declines with the same  $\tau_{\rm K_{II}}$  for all  $E_1$  as in Type I fibers. The delay thus appears to be an additional process, which develops or becomes apparent at larger prepulses  $E_1$ . The delays are not observed at less negative test pulses. In this experiment the next to -104 mV value of  $E_2$  was -83 mV, and the components  $I_{\rm K_{I}}$  and  $I_{\rm K_{II}}$  of  $I_{\rm K}$  tails associated with different  $E_1$  and  $E_2=-83$  mV were in all respects like those in Figs. 1 and 4. These fibers thus behave in accordance with the HH formalism only in a certain range of  $E_1$  and  $E_2$ .

1.3. Type III fibers. The behavior of these relatively rare fibers is exemplified in Fig. 10.  $I_{\rm K}$  tails decay exponentially (the top), and  $I_{\rm K}-t$  curves shift in parallel along the t-axis as prepulse amplitude is changed (the bottom), in full accordance with Eqs. (7-8). For 12 different  $E_1$  ranged from 60 to  $-60\,{\rm mV}$  (here  $E_2$  was  $-98\,{\rm mV}$ ),  $\tau_{\rm K}$  was  $0.995\pm0.015\,{\rm msec}$  (mean  $\pm{\rm sp}$ , n=12, see column 2 in Table 2). At  $E_2\sim-100\,{\rm mV}$  the rate of decay of the  $I_{\rm K}$  tail of this node

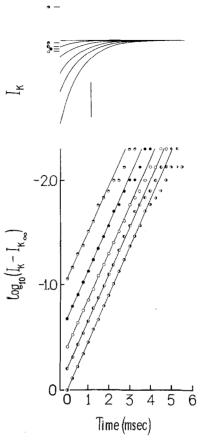


Fig. 10. The Cole-Moore test for repolarization in a Type III fiber. Above:  $I_{\rm K}$  tails associated with steps from  $E_1$  (downwards from the base-line): -60, -48, -35, -14, and +60 mV to  $E_2=-98$  mV.  $I_{\rm K}$  levels immediately before a step at these  $E_1$  values are indicated by symbols  $\bullet$ ,  $\bullet$ ,  $\circ$ ,  $\bullet$ ,  $\circ$ , respectively. Duration of  $E_1$ , 50 msec. Note that the  $I_{\rm K}$  tails are parallel which is better seen from graphical analysis below. Below: graphical analysis of the  $I_{\rm K}$  tails above. All the details as in Fig. 1. For time constants, see Table 2, column 2. For relative values of amplitudes of instantaneous currents on the linear scale, see Fig. 5A. Node 518

was the same as that of the  $I_{K_I}$  current in Type I fibers. The  $g_{K_\infty}-E$  relationship here (half-filled circles in Fig. 5A) was also the same as  $g_{K_{I\infty}}-E$  relationship in Type I fibres. These facts suggest that  $I_K$  of the node of Fig. 10 is an uncomplicated  $I_{K_I}$  current, i.e. in Type III fibers the slow current  $I_{K_{II}}$  is lacking.

## 2. K Currents at Repolarization: Analysis

Two exponential decay of  $g_K$  in Type I (most numerous) fibers and the shapes of the steady-state values and relaxation times as functions of E for both components can be accounted for by the assumption that the node usually comprises two dynamic HH K channels with different kinetics and E dependency. The same refers to linearity of instantaneous current-

voltage characteristics of both components. On the other hand, the dual exponential decay of  $g_K$  and practically all the above features, when considered separately, may also be accounted for by a three-state model for the K channel. Such a model was recently elegantly used by Chiu (1977) to describe Na inactivation in the frog nerve: an S-shape time course of recovery from and dual exponential development of inactivation. In multiple-state models, however,  $g_{K_I}$  and  $g_{K_{II}}$  will be coupled and the parameters characterizing them will be interrelated. We shall now show that the interrelation required by the models is not observed in experiment.

Let us consider three-state scheme (10)

$$1 = \frac{a_1}{b_1} 2 = \frac{a_2}{b_2} 3$$

$$n_1 + n_2 + n_3 = 1$$
(10)

where  $a_i$  and  $b_i$  are E-dependent forward and backward rate constants, respectively, and of the three states only one is conducting. Since on repolarization the system starts from the conducting state, it is convenient to take this state to be state 1, that is  $g_K(t) \sim n_1(t)$ . Scheme (10) is described by two independent linear differential equations yielding the following general solution for  $n_1(t)$ 

$$n_1(t) = G_{11} \exp(-k_1 t) + G_{12} \exp(-k_2 t) + n_{1\infty}$$
 (11)

where  $k_1$  and  $k_2$  are reciprocal relaxation times in every kinetic response obtained as eigenvalues from the characteristic equation,  $G_{11}$  and  $G_{12}$  are amplitude coefficients of the exponential terms defined from initial conditions and expressed as

$$G_{11} = \frac{(a_1 + b_1 - k_2)(n_{10} - n_{1\infty}) + b_1(n_{30} - n_{3\infty})}{k_2 - k_1}$$
(12)

$$G_{12} = \frac{(a_1 + b_1 - k_1)(n_{10} - n_{1\infty}) + b_1(n_{30} - n_{3\infty})}{k_1 - k_2}$$
 (13)

and

$$n_{1\infty} = b_1 b_2 / (a_1 a_2 + a_1 b_2 + b_1 b_2). \tag{14}$$

In a repolarization kinetic response all the parameters entering Eq. (11) are experimentally measured quantities:  $k_{1,2} = 1/\tau_{K_{\rm I,I}}$  or  $k_{1,2} = 1/\tau_{K_{\rm II,I}}$ ;  $G_{11} = g_{K_{\rm IO}}$ ,  $G_{12} = g_{K_{\rm IIO}}$  or vv;  $n_1 = g_{K_{\infty}}$  (with  $\bar{g}_{\rm K}$  normalized to 1, which will be assumed throughout the analysis).

The repolarization data obtained for Type I fibers are characterized by three main features. (i)  $\tau_{K_1}$  and  $\tau_{K_1}$  are independent of  $E_1$  (Table 2). This is true for any monomolecular reaction because  $k_1$  and  $k_2$  are only defined by  $a_i$  and  $b_i$  which do not depend on  $E_1$ . It is obvious then that independent translation of

each  $g_{\rm K}$  component alone cannot be the basis for discrimination between one-channel and two-channel models. The other two features are of greater utility in this respect. They are: (ii)  $g_{\rm K_{10}}$  and  $g_{\rm K_{110}}$  do not depend on  $E_2$ ; that is, the ratio  $g_{\rm K_{10}}/g_{\rm K_{110}}$  is constant at all  $E_2$  values (Fig. 7); (iii)  $\tau_{\rm K_{1}}$  and  $\tau_{\rm K_{11}}$  depend on  $E_2$  in such a way that  $\tau_{\rm K_{11}}-E$  and  $\tau_{\rm K_{11}}-E$  relationships when plotted to the same vertical scale (msec) are not parallel (it follows from Figs. 2-3 or Fig. 8 A, B).

Consider feature ii. Figure 6 says that  $g_{K_{-}} \rightarrow 0$ when  $E_2$  is in the vicinity of  $-100 \,\mathrm{mV}$ . The condition  $g_{K_{\infty}} = 0$  means that  $n_{1\infty} = 0$ . It can be shown (Makovsky, 1979) that the latter condition imposes constraints on  $a_i$ ,  $b_i$  such that  $k_1$  and  $k_2$  obtained from the characteristic equation and introduced into Eqs. (12)-(13) give either  $G_{11}$  or  $G_{12}$  tending to zero. Whether this will be the amplitude coefficient of the fast or slow term in Eq. (11) depends on whether the first forward transition in scheme (10) is respectively slow  $(a_1 < a_2)$  or fast  $(a_1 > a_2)$ . Thus with sufficiently large and negative  $E_2$ , mono-exponential kinetics must be observed. This prediction of three-state model (completely fulfilled for dual-exponential development of the Na channel inactivation in frog nerve (Chiu, 1977)) does not, however, agree with experimental data of Figs. 1 and 4.

Feature iii allows another test of the model. The data of Fig. 7 were obtained with  $E_1 = 67$  mV, that is with  $n_{10} = 1$  (see Fig. 5A) and  $n_{30} = 0$ . Again in the vicinity of -100 mV,  $n_{1\infty} = 0$  and  $n_{3\infty} = 1$ . Then in this E range, one must have

$$\frac{g_{K_{I0}}}{g_{K_{II0}}} = \frac{G_{11}}{G_{12}} = \frac{a_1(E) - k_2(E)}{k_1(E) - a_1(E)} = \text{const},$$
(15)

and  $\tau_{K_I} - E$  and  $\tau_{K_{II}} - E$  plots should have then been parallel; they were not.

Thus the three-state mechanism with one conducting state cannot explain the dual-exponential decline of  $g_K$  and, as a consequence, the dependence of  $g_K$  kinetics on initial conditions.

In general, an x-state scheme yields (x-1) exponentials. If, again, only the first state is conducting, then (as  $\bar{g}_K$  is taken to be 1)

$$g_{\mathbf{K}}(t) = n_1(t) = \sum_{i=1}^{x-1} G_{1i} \exp(-k_i t) + n_{1\infty}.$$

In applying this formula to our experimental results we should assume that either (x-3) amplitudes are negligibly small or (x-3) values from the set of  $k_i$  are much larger than the other two. Besides, with  $E_1$  large and positive (when  $g_{K_{\infty}}=1$ ) and  $E_2$  large and negative (when  $g_{K_{\infty}}=0$ ) all  $n_{i0}$ , except  $n_{10}(=1)$  will be 0 and so will be all  $n_{i\infty}$ , except  $n_{\infty}(=1)$ . Then expressing the ratio  $g_{K_{10}}/g_{K_{110}}$  through rate constants

 $a_i$  and  $b_i$  one must obtain an expression similar to Eq. (15). We can thus conclude that multiple-state models with one conducting state are not likely to describe our experimental results.

The linearity of current-voltage characteristics in Fig. 6 suggests the possibility of a process with two conducting states. Let these states, in model (10), be states 1 and 2. Then

$$\begin{split} &g_{\mathbf{K}}(t) = n_1(t) + n_2(t) \\ &= (G_{11} + G_{21}) \exp(-k_1 t) + (G_{12} + G_{22}) \exp(-k_2 t) \\ &+ G_{22} \end{split}$$

where  $G_{21}$  and  $G_{22}$  are amplitude coefficients relating to state 2. It can be shown (Makovsky, 1979) that the condition  $G_{\infty}=0$  gives  $b_2=0$  in Eq. (14), and this leads to  $k_{1,2}=a_{1,2}$  or  $k_{1,2}=a_{2,1}$ . With  $E_1$  sufficiently large and positive and  $E_2$  sufficiently large and negative,  $n_{30}=0$  and  $n_{3\infty}=1$ . It can also be shown then (Makovsky, 1979) that

$$\frac{g_{K_{10}}}{g_{K_{110}}} = \frac{n_{10}}{n_{20}} = \frac{a_2(E) - n_{10} k_2(E)}{n_{10} k_1(E) - a_2(E)} = \text{const.}$$

As  $n_{10} \neq 0$ , this ratio is always more than zero and less than infinity. This means that dual-exponential decay of  $g_K$  can be observed even at extreme negative values  $E_2$  and at any relative values of conductances in states 1 and 2, but the predicted  $\tau_{K_1} - E$  and  $\tau_{K_1} - E$  plots (which proves to be parallel again) do not agree with experiment. Of course, in a model with two conducting states no less than four states are needed to account for depolarization delay of  $g_K$  turn on kinetics. But we do not believe these models to be likely either, for the same reasons as discussed above for multiple-state models with one conducting state.

The failure of multiple-state models to account for dual-exponential decay of  $g_K$  in the present experiments is evident. As was noted above, in these models  $g_{K_I}$  and  $g_{K_{II}}$  are coupled and the parameters characterizing them are interrelated. In our experiments, however, no coupling was observed.

## 3. K Currents at Depolarization: Results

3.1. Type I Fibers. Fig. 11 shows  $I_K-t$  curves associated with depolarizing steps, under the Cole-Moore conditions, for a fiber belonging to Type I according to classification given in section 1.1. In this experiment the node was in high K solution 4. Altogether there were 12 different prepulses  $E_1$  and the same test pulse  $E_2$ . The curves obtained are spaced 0.25 msec apart for clarity. It can be seen that, in accordance with Eqs. (5)-(6), the curves shift to the right along the t-axis with more negative  $E_1$  but the

shifts are non-parallel: the more negative is  $E_1$ , the more slowly curves rise.  $I_{\rm K}-t$  curves of this type were observed with all  $E_2$  applied (between about  $-30 \div 60 \, {\rm mV}$  in 2.5 mM KCl and  $10 \div 60 \, {\rm mV}$  in 128mM KCl). Similar results have also been reported by others for R. esculenta (Palti et al., 1976).

It might be assumed (although not easily explained) that this dependence of  $I_{\rm K}$  kinetics on initial conditions is due to  $E_1$  dependence of the HH time constant  $\tau_n$ . Had this been so, the  $I_{\rm K}-t$  curves of Fig. 11 plotted as  $\ln(1-I_{\rm K}^{1/x})$  against t (with  $I_{\rm K\infty}$  taken to be 1) should have been straight, if not parallel, lines, if the value of x were properly adjusted (this follows from Eqs. (3)-(4), if  $E_{\rm K}=$  const which was shown above to be really the case). No such value of x could be found, which means that  $I_{\rm K}$  kinetics in this case cannot be presented by  $n^x$  formalism at all. The same conclusion has also been drawn by Palti et al. (1976) for analogous  $I_{\rm K}-t$  curves with R. esculenta.

3.2. Type II Fibers. On depolarization,  $I_{\rm K}$  kinetics in these fibers were practically indistinguishable from those of Type I fibers. This result is consistent with the fact that the difference between the two types of fibers could be detected only with sufficiently negative test potentials (section 1.2).

3.3. Type III Fibers. In fibers of this type under the same experimental conditions as in Fig. 11  $I_{\rm K}-t$  curves shift in parallel; i.e., the Cole-Moore translation of  $g_{\rm K}$  is observed directly. Analogous results were obtained with different  $E_2$  (23, 42, and 60 mV) (not shown).

The  $I_{K}-t$  curves associated with the same  $E_{1}$ (-98 mV) and various  $E_2$  (ranged from -60 to 60 mV) could be made to superimpose by double translation along coordinates  $\log I_{K}$  and  $\log t$  (Makovsky, 1979), which means that in Type III fibers  $I_K$  kinetics can be described by the  $n^x$  formalism (Dodge 1963; Hille 1967a). Figure 12 presents five of these  $I_K$  curves plotted as  $\ln(1-I_K^{1/x})$  against t (from the same node as in Fig. 10). One can clearly see that plots are linear with all  $E_2$  used and with x=4 only. With smaller x (2) the curves displayed, at small t, a positive curvature and with greater t (5 or 6) a negative curvature (not shown). The same value of x=4 was found with all other  $E_2$  (-60, -40, -20, 50 mV) and with different  $E_1$  (-60, -32 mV); that means x = 4 is the correct value of x in Eq. (4).

#### 4. K Currents at Depolarization: Analysis

On depolarization,  $I_K$  currents in Type III fibers obey  $n^4$  kinetics and do not require special treatment. It is

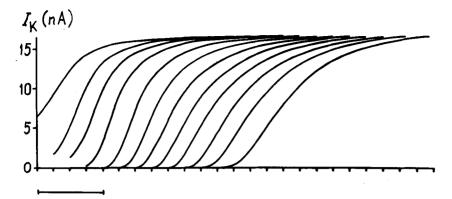


Fig. 11. The Cole-Moore test for depolarization in a Type I fiber. The  $I_{\rm K}-t$  curves are spaced apart at 0.25 msec for clarity.  $E_1$  (running from left to right): -32, -50, -55, -65, -75, -88, -103, -113, -120, -132, -146, and -170 mV.  $E_2$  (10 msec) was +50 mV. (For other details, see text.) Note that the  $I_{\rm K}-t$  curves are nonparallel. 128 mM KCl Ringer  $+3\cdot10^{-4}$  mm TTX. Leakage current was subtracted. Calibration time bar: 1 msec. Node 146

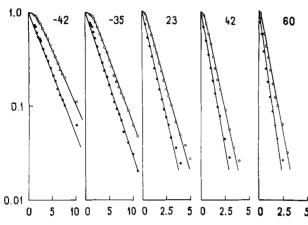


Fig. 12.  $I_{\rm K}-t$  curves of a Type III fiber associated with E steps from  $E_1$  (-98) to 5  $E_2$  indicated near the curves plotted as  $\ln(1-I_{\rm K}^{1/x})$  against  $t. \circ -x=2$ ; • - x=4. 128 mM KCl Ringer  $+3\cdot 10^{-4}$  mM TTX. Node 518

sufficient to note that  $\tau_n - E$  and  $n_\infty - E$  relationships were obtained from  $\ln(I_{K_\infty}^{1/4} - I_K^{1/4}) - t$  plots (Makovsky, 1979) and proved to be very near to those in R. pipiens (Dodge, 1963; Hille, 1967a). Again, repolarization data indicate that the fast component  $I_{K_{\rm II}}$  is invariant with respect to the type of a fiber and it is not coupled to the slow component  $I_{K_{\rm II}}$ . These facts and the mode of action of TEA (Section 5) suggest that  $I_{K_{\rm II}}$  and  $I_{K_{\rm II}}$  are due to separate K channels, a fast and a slow.

Depolarization data for Type III fibers further suggest that the fast channel is the familiar  $n^4$  channel of R. pipiens. The slow channel, at least in most fibers, is also of the HH type: repolarization data show that it is controlled by a single first-order variable, and its steady-state and kinetic characteristics are like those in HH. In essence, the only unknown parameter for the slow channel remains the value of x.

On the basis of these data we attempted to represent  $I_{\rm K}$  of Type I fibers in Fig. 11 as the sum of two HH currents,  $I_{\rm K_I}$  and  $I_{\rm K_{II}}$ . If, as above, we take  $I_{\rm K_I}$  as

the fast current, then  $x_{\rm I}$  and ratio  $\bar{g}_{\rm K_{\rm II}}/\bar{g}_{\rm K_{\rm I}}$  could be considered known. However, we did not use them. Instead, we tried to find all the HH parameters with least squares and compare them to observations.

The model analyzed was as follows.

$$\begin{split} &I_{\mathbf{K}} = I_{\mathbf{K}_{\mathbf{I}}} + I_{\mathbf{K}_{\mathbf{II}}} \\ &I_{\mathbf{K}_{\mathbf{I}}} = g_{\mathbf{K}_{\mathbf{I}}} (E - E_{\mathbf{K}_{\mathbf{I}}}) \\ &I_{\mathbf{K}_{\mathbf{II}}} = g_{\mathbf{K}_{\mathbf{II}}} (E - E_{\mathbf{K}_{\mathbf{II}}}) \\ &g_{\mathbf{K}_{\mathbf{I}}} = \overline{g}_{\mathbf{K}_{\mathbf{I}}} \cdot n_{\mathbf{I}}^{\mathbf{x}_{\mathbf{I}}} \\ &g_{\mathbf{K}_{\mathbf{II}}} = \overline{g}_{\mathbf{K}_{\mathbf{II}}} \cdot n_{\mathbf{II}}^{\mathbf{x}_{\mathbf{II}}}. \end{split}$$

As under the conditions we used  $E_{K_I} = E_{K_{II}} = \text{const}$  (Fig. 7), and the above equations yielded:

$$g_{\mathbf{K}} = g_{\mathbf{K}_{\mathbf{I}}} + g_{\mathbf{K}_{\mathbf{II}}}.\tag{16}$$

Further obvious assumptions were that at E = 50 mV,  $n_{I_{\infty}} = n_{II_{\infty}} = 1$ : they followed from Fig. 5A and B. Eq. (16) then acquired the form

$$g_{K}(t) = \bar{g}_{K_{I}} \left[ 1 - (1 - n_{I_{\infty}}(E_{1})) \exp\left(-\frac{t}{\tau_{n_{I}}}\right) \right]^{x_{I}} + \bar{g}_{K_{II}} \left[ 1 - (1 - n_{II_{\infty}}(E_{1})) \exp\left(-\frac{t}{\tau_{n_{I}}}\right) \right]^{x_{II}}.$$
 (17)

To estimate a possible position of the absolute minimum we first fitted Eq. (17) to individual curves in Fig. 11. The calculated parameters of the curves behaved with  $E_1$  just as predicted by the HH model:  $x_{\rm I}$  and  $x_{\rm II}$  (both 4) as well as  $\bar{g}_{\rm K_{\rm I}}$  and  $\bar{g}_{\rm K_{\rm II}}$  were constant within a few percent and so practically were  $\tau_{n_{\rm I}}$  and  $\tau_{n_{\rm II}}$ , at least with moderate  $E_1$ ;  $n_{\rm I_{\infty}}$  and  $n_{\rm II_{\infty}}$  increased with  $E_1$  (Table 3). The values found were then taken as coordinates of the starting point of the descent in the search of the absolute minimum of variance under the constraint that  $\bar{g}_{\rm K_{\rm I}}$ ,  $\bar{g}_{\rm K_{\rm II}}$  and  $\tau_{n_{\rm I}}$ ,  $\tau_{n_{\rm II}}$  were the same for all 12 curves. The simultaneous fitting yielded  $x_{\rm I} = x_{\rm II} = 4$ ;  $\bar{g}_{\rm K_{\rm I}} = 0.61$ ,  $\bar{g}_{\rm K_{\rm II}} = 0.39$ ;  $\tau_{n_{\rm I}} = 0.24$  msec,  $\tau_{n_{\rm II}} = 0.69$  msec;  $n_{\rm I_{\infty}}$  and  $n_{\rm II_{\infty}}$  depended then on  $E_1$  as shown in Fig. 13. With these values the  $I_{\rm K} - t$  curves in Fig. 11 were fitted to line thickness.

Table 3

E <sub>1</sub> (mV)	-32	-50	-55	-65	-75		-103	-113	-120	-132	-146	-170
$\bar{g}_{\mathbf{K}_{\mathbf{I}}}$	0.63	0.61	0.61	0.61	0.61	0.61	0.60	0.60	0.61	0.60	0.60	0.60
$\bar{g}_{K_{II}}$	0.37	0.39	0.39	0.39	0.39	0.39	0.40	0.40	0.39	0.40	0.40	0.40
$n_{I_{\infty}}$	0.48	0.17	0.01	0.07	0.02	0.05	0.03	0.02	0.00	0.00	0.00	0.00
$n_{\mathrm{H}_{\infty}}$	1.00	0.83	0.81	0.60	0.43	0.31	0.20	0.11	0.08	0.03	0.00	0.00
$\tau_m$ (msec)	0.32	0.26	0.24	0.23	0.24	0.25	0.25	0.27	0.33	0.35	0.44	0.45
$\tau_{nu}$ (msec)	0.62	0.62	0.62	0.62	0.64	0.65	0.70	0.73	0.75	0.80	0.81	0.81

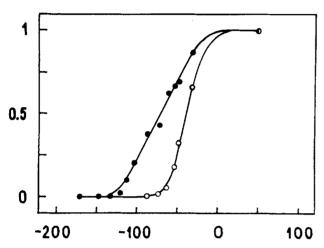


Fig. 13.  $n_{\text{L}_{\infty}}-E$  (open circles) and  $n_{\text{H}_{\infty}}-E$  (filled circles) relationships obtained from fitting Eq. (18). E values from -170 to -32 mV are the  $E_1$  values shown in Fig. 11; E=+50 mV is  $E_2$  in Fig. 11. (For details of computation, see text)

One can easily see that the predictions of the modified HH model are fully consistent with the data measurable in direct experiment: the fast component  $g_{K_I}$  makes a larger contribution to  $g_K$ , is activated by a somewhat more positive E range and depends more strongly on E as compared with the slow component  $g_{K_{II}}$  (repolarization data of Fig. 5), and  $x_I$  has the correct value of 4. It is therefore very likely that the slow channel kinetics can also be described as  $n^4$ .

In the present study initial depolarization conditions were changed by varying the prepulse amplitude. Somewhat more complicated results have been obtained by Ganot et al. (1978) with varying prepulse duration. Our unpublished calculations, analogous to those described above, show that the model proposed could account for most of their results; furthermore,  $x_1 = x_{II} = 4$  were found to give the best fit.

## 5. The Mode of Action of TEA

The detailed report of these experiments will be published elsewhere, and now we will only summarize data relevant to the results of the kinetic analysis presented above.

In Type III fibers TEA failed to affect the  $g_K$  kinetics either at depolarization or repolarization, and its action, including the dose-effect curve, was the same as that reported by Hille (1967a, b) for R. pipiens.

Type II fibers were not encountered in these experiments. In Type I fibers, on repolarization, TEA did not change  $\tau_{K_I}$  and  $\tau_{K_{II}}$  but appreciably increased the ratio  $\overline{g}_{K_{II}}/\overline{g}_{K_{I}}$ , suggesting that the fast component  $g_{K_{II}}$  was several times more sensitive to TEA than the slow component  $g_{K_{II}}$ . On depolarization, TEA lengthened the rate of rise of  $I_K-t$  curves in these fibers in much the same way reported by Koppenhöfer (1967) for X. laevis. Estimates showed that this lengthening could be accounted for by smaller contribution of the fast component to the overall  $I_K$  in the presence of TEA. The data of the pharmacological analysis are thus in full agreement with those obtained in the kinetic analysis.

## Discussion

The results obtained in the present study can be summarized as follows. In contrast to R. pipiens, in most R. ridibunda nerve fibers there is an additional, slow K current component uncoupled to the fast component  $n^4$  (termed here  $n_1^4$  component). The turning on of this slow component can also be described by  $n^4$  kinetics (and this component is termed  $n_{\rm II}^4$ ), although on repolarization its turn-off kinetics sometimes reveal an additional process preceding the exponential decline. It is this slow component that brings about the nontranslational behavior of  $I_{\kappa}$ . The component was attributed to a slow K channel while the fast K channel appears to be the same as in R. pipiens. The action of TEA is fully consistent with this two-K-channel picture, the slow channel being less sensitive to TEA than the fast channel.

Although differential action of TEA on the fast and slow K currents provides further strong evidence for two different K channels, it would be interesting to find a representation which could cover the results obtained within a one-K-channel model.

We tried some models but without success. Besides multiple-state models considered briefly in section 2, depolarization data taken separately might be accounted for by many models. Among them the most simple are those based on modification of the original HH model, such as supplementation of the  $n^4$  kinetics by some additional process or introduction of cooperative interaction between the HH nsubunits. Repolarization data, however, indicate that these modifications are unlikely condidates. In the first model we could not obtain constant ratio  $g_{K_{\rm IO}}/g_{K_{\rm IIO}}$  with different repolarizing test potentials, as in Fig. 7, and in the second model, according to calculations of Hill and Chen (1971a),  $g_{K}$  "decreases, typically in a repolarization, following a more or less first-order curve."

The ability of the HH formulation to describe novel results is very impressive, but there are two points concerning the present experiments in which the model is inadequate. First, and most important, the appearance, at extreme initial and final potentials. of a delay preceding exponential decline of the slow K current on repolarization, in Type II fibers indicates that the HH kinetics are only a special case of some kinetics of a more general type. As depolarization data are not easy to use to reveal and assess possible kinetic difference between  $g_{K_I}$  and  $g_{K_{II}}$  in Type I and Type II fibers, we did not attempt to construct a general model, but we consider it an important matter. All that we can say now is that a three-state model for a slow K channel with  $k_1 = k_2$ =k, giving  $(G_{11}+tG_{12}) \exp(-kt)+n_{1\infty}$  as the general solution to scheme (10), with a delay when t is small and exponential decay when t is large, does not account for the observed E-dependence of the delay. The other point is dependence of  $\tau_{n_{\rm I}}$  and  $\tau_{n_{\rm II}}$  on extreme initial hyperpolarizing potentials (Table 3). Its lengthening with more negative  $E_1$  is not the result of separate processing of the curves, and it is not likely that it was due to a damaging effect of large hyperpolarization. Though this effect may be considered unimportant for usual experimental situations, it is interesting because in squid such dependence was not observed (Cole & Moore, 1960). It would be of interest to check the possibility of whether such an effect might be produced by some interaction imposed on n-subunits by strong initial hyperpolarization.

Having postulated that, in general, a K channel either fast or slow obeys  $n^x$  formalism, i.e., it displays the properties of translation and induction, one can infer, following theoretical analysis of Hill and Chen

(1971 a, b), that cooperative interaction either of gating subunits within a channel or between the channels cannot be the basis for such kinetics; experimental data of Sigworth (1979) seem to agree with this conclusion. Aggregation models, at least simple ones, are not likely either (Hill & Chen, 1971b). As  $g_K - t$  curves cannot be used to distinguish between the classical HH model (k=0) and k-models of Hill and Chen (1972; Chen, 1976), both single-conductance (HH) and multiple-conductance (Hill & Chen) mechanisms are possible for fast and slow K channels.

The coupling between the K channels and Na channels (Mullins, 1968) is strongly excluded because Hoyt (1971) has shown that the property of translation (displayed by the K current) and inactivation (displayed by the Na current) cannot be coupled. For this same reason the activation and inactivation properties within the fast K channel observed in the present work must be uncoupled, too. As to the difference between the fast and slow K channels it might be due mostly to different heights of the activation energies and/or the effective charge of gating subunits. It can be noted that an EIM channel has very different relaxation times in different lipid bilayers (Bean, 1973).

The role of fast and slow K channels with the properties we have measured was studied in the repetitiveness of amphibian sensory fibers (Makovsky, 1979). Spike trains were computed on the basis of the Dodge-HH model (Hille, 1967a) modified to cover the  $g_{Krr}$  component. The results obtained (Krylov & Makovsky, 1978, 1979) show that the K channels are important for analog-code input-output transformation of a signal. The fast channels appear to be mostly responsible for the output frequency as a logarithmic function of constant current strength (Bromm & Frankenhaeuser, 1972). The slow channels ensure spike frequency adaptation (increase in time of interspike intervals during the action of a maintained stimulus) and numeric coding (increase in number of spikes in a discharge with stimulus strength). Spike frequency adaptation has previously been shown to be due to a slow K channel in molluscan neurones (Partridge & Stevens, 1976). Although both types of aperiodic processes in amphibian sensory fibers experimentally are well known (Erlanger & Blair, 1938; Dodge, 1963; Vallbo, 1964a, b; Honerjäger, 1968; Bergman, 1969; see also literature in Stämpfli & Hille, 1976), they failed to be described in terms of the HH model for the node (Dodge, 1963; Frankenhaeuser & Vallbo, 1965). By contrast, consideration of the slow K channel not only accounts for these processes as such but also for their variability in different amphibian fibers (well known by experimentors and studied by Vallbo, 1964a), when variability

in the properties of slow K channels as described in the present study are taken into account. As the coding properties of fibers for different senses must differ, the variability of the density of the slow K channels must be of physiological value. It is interesting to note that previously the role of the dynamic K channels has been considered unknown because they do not practically participate in repolarization of the excited membrane of the node (Dodge, 1963; Frankenhaeuser & Huxley, 1964; Khodorov, 1975).

To summarize, we conclude that in R. ridibunda node the departure of the  $g_K$  behavior from the HH kinetics is due to the involvement of a slow K channel. The same may be true for other amphibia where the Cole-Moore effect is not observed (Makovsky, 1975; Palti et al., 1976; Ganot et al., 1978). In R. pipiens both the Cole-Moore and other tests (Dodge, 1963; Hille, 1967a) give no indication of such channels. However, here spike frequency adaptation is also observed (Dodge, 1963). A possible source for this adaptation might be slow Na inactivation described by Chiu (1977), but clear-cut increase in the undershoot amplitudes with time makes one suspect the involvement of a slow K system. If  $E_{K_{TI}}$  of this system would be as large as the resting potential which amounts to -81 mV (Campbell & Hille, 1976), then under certain conditions  $g_{K_\Pi}$  as small as only 10% of  $g_{K_1}$  could produce pronounced adaptation. We feel therefore that it is worthwhile to look for a slow K system in R. pipiens node under voltage clamp conditions. Either result might be useful in interpretation of  $I_{K}$  noise measurements (cf. Begenisich & Stevens, 1975; Chen, 1976).

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#### Note in Proof

This paper was published posthumously after the untimely death of V.S. Makovsky.

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